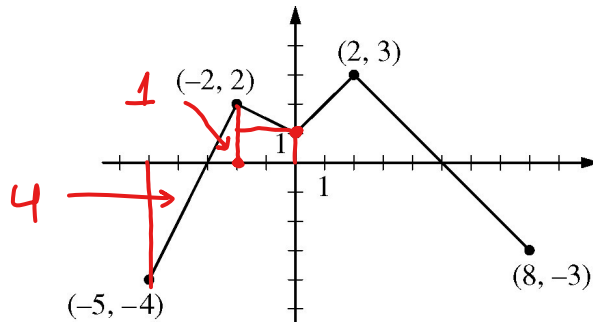


NO CALCULATOR ALLOWED

Graph of f

4. The continuous function f is defined on the interval $-5 \leq x \leq 8$. The graph of f , which consists of four line segments, is shown in the figure above. Let g be the function given by $g(x) = 2x + \int_{-2}^x f(t) dt$.

(a) Find $g(0)$ and $g(-5)$.

$$g(0) = 2(0) + \int_{-2}^0 f(t) dt = 0 + 2 + 1 = 3$$

$$g(-5) = 2(-5) + \int_{-2}^{-5} f(t) dt = -10 - 1 + 4 = -7$$

(b) Find $g'(x)$ in terms of $f(x)$. For each of $g''(4)$ and $g''(-2)$, find the value or state that it does not exist.

$$g'(x) = 2 + f(x)$$

$$g''(x) = f'(x)$$

$$g''(4) = f'(4) = \frac{-6}{6} = -1$$

$$g''(-2) = f'(-2) \text{ Does not exist}$$

Do not write beyond this border.

Do not write beyond this border.

4

4

4

4

4

4

4

4

4

4

NO CALCULATOR ALLOWED

(c) On what intervals, if any, is the graph of g concave down? Give a reason for your answer.

$g'' < 0$
 $(-2, 0)$ $(2, 8)$

↓ OR
 f' is negative
 OR
 f is decreasing

(d) The function h is given by $h(x) = g(x^3 + 1)$. Find $h'(1)$. Show the work that leads to your answer.

Composition
 require chain rule

$$h'(x) = g'(x^3 + 1) \cdot (3x^2)$$

$$h'(1) = g'(1^3 + 1) \cdot (3 \cdot 1^2)$$

$$= g'(2) (3)$$

↓

$$[2 + f(2)] [3]$$

$$[2 + 3] [3] = \boxed{15}$$