

(d) $\int_0^3 r(t) dt = 973$
2008 AP® CALCULUS AB FREE-RESPONSE QUESTIONS

t (hours)	0	1	3	4	7	8	9
$L(t)$ (people)	120	156	176	126	150	80	0

2. Concert tickets went on sale at noon ($t = 0$) and were sold out within 9 hours. The number of people waiting in line to purchase tickets at time t is modeled by a twice-differentiable function L for $0 \leq t \leq 9$. Values of $L(t)$ at various times t are shown in the table above.

- (a) Use the data in the table to estimate the rate at which the number of people waiting in line was changing at 5:30 P.M. ($t = 5.5$). Show the computations that lead to your answer. Indicate units of measure.
- (b) Use a trapezoidal sum with three subintervals to estimate the average number of people waiting in line during the first 4 hours that tickets were on sale.
- (c) For $0 \leq t \leq 9$, what is the fewest number of times at which $L'(t)$ must equal 0? Give a reason for your answer.
- (d) The rate at which tickets were sold for $0 \leq t \leq 9$ is modeled by $r(t) = 550te^{-1/2}$ tickets per hour. Based on the model, how many tickets were sold by 3 P.M. ($t = 3$), to the nearest whole number?

(a)
$$\frac{150 - 126}{7 - 4} = 8 \text{ people/hr}$$

(b)
$$\frac{(\frac{1}{2})(120 + 156)(1) + (\frac{1}{2})(156 + 176)(2) + (\frac{1}{2})(176 + 126)(1)}{4 - 0}$$

(c) 3 times $L(t)$ changes inc to dec and then dec to inc, then inc to dec
 and $L(t)$ changes inc \rightarrow dec or dec \rightarrow inc if

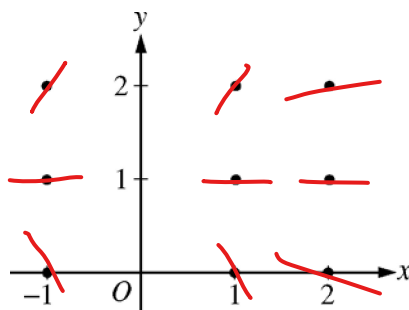
$$L'(t) = 0 \quad \text{IVT}$$

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5. Consider the differential equation $\frac{dy}{dx} = \frac{y-1}{x^2}$, where $x \neq 0$.

(a) On the axes provided, sketch a slope field for the given differential equation at the nine points indicated.

(Note: Use the axes provided in the exam booklet.)



(b) Find the particular solution $y = f(x)$ to the differential equation with the initial condition $f(2) = 0$.

(c) For the particular solution $y = f(x)$ described in part (b), find $\lim_{x \rightarrow \infty} f(x)$.

$$\frac{dy}{dx} = \frac{y-1}{x^2}$$

$$\int \frac{dy}{y-1} = \int \frac{1}{x^2} dx \rightarrow 1x^{-2}$$

$$\ln|y-1| = -\frac{1}{x} + C$$

$$\ln|0-1| = -\frac{1}{2} + C$$

$$0 = -\frac{1}{2} + C$$

$$C = \frac{1}{2}$$

$$\ln|y-1| = -\frac{1}{x} + \frac{1}{2}$$

$$e^{\ln|y-1|} = e^{-\frac{1}{x} + \frac{1}{2}}$$

$$y-1 = -e^{-\frac{1}{x} + \frac{1}{2}}$$

$$y = -e^{-\frac{1}{x} + \frac{1}{2}} + 1$$

(c) $\lim_{x \rightarrow \infty} f(x) = -e^{\frac{1}{2}} + 1$

END OF EXAM