BC Calculus Polar Area Notesheet

We are going to look at areas enclosed by polar curves, that's enclosed, not under as we typically have in these problems. These problems work a little differently in polar coordinates. Here is a sketch of what the area that we'll be finding in this section looks like.

The formula for polar area is different from all previous area formulas, because it is not based on rectangles. Instead, polar area uses an infinite number of sectors to find the area. Remember that a sector is a hunk of a circle, a slice of pizza from the whole pizza.

The area of a sector of a circle is given by $A = \frac{1}{2}\theta r^2$, where θ is measured in radians. Our area is bounded by the radial lines from $\theta = \alpha$ to $\theta = \beta$.





Example 2 Find the area of one petal of $r = 2 \sin(3\theta)$

Example 3 Find the area of one petal of $r = \cos(2\theta)$

Example 4 Find the area inside one loop of $r^2 = 4 \cos(2\theta)$





a) Find the area bounded by the curve and the x-axis.

- **b)** Find the angle θ that corresponds to the point on the curve where x = -2.
- **c)** For $\frac{\pi}{3} < \theta < \frac{2\pi}{3}$, $\frac{dr}{d\theta}$ is negative. What does this say about the graph on this interval?

d) At what angle θ in the interval $0 \le \theta \le \frac{\pi}{2}$ is the curve farthest away from the origin? Justify your answer.