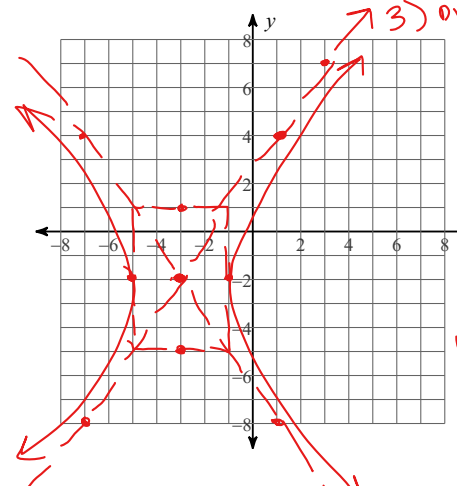


Conic Sections Hyperbolas Notes

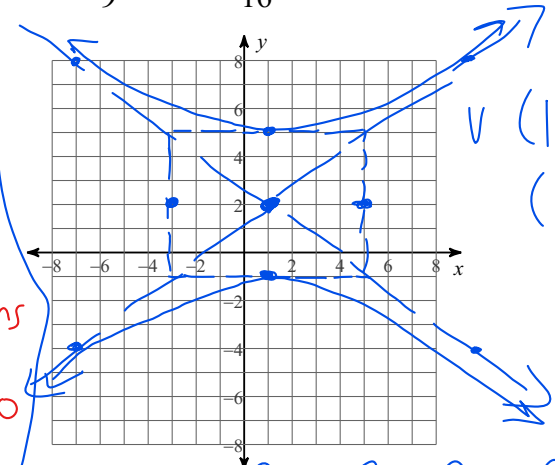
Identify the vertices, foci, and asymptotes of each. Then sketch the graph.

1)  $\frac{(x+3)^2}{4} - \frac{(y+2)^2}{9} = 1$



- 1) "center" (-3, -2)
- 2) Find x-y distances
- 3) draw a rectangle
- 4) Draw the diagonals through the corners (asymptotes)
- 4) Figure out if the hyp opens up/down or L/R? (which one(x or y) > 0)

2)  $\frac{(y-2)^2}{9} - \frac{(x-1)^2}{16} = 1$



- "center" (1, 2)
- V (1, -1)
- (1, 5)

$c^2 = a^2 + b^2 = 9 + 16 = 25$   
 $c^2 = 25$  so  $c = 5$   
 Foci (1, -3) (1, 7)

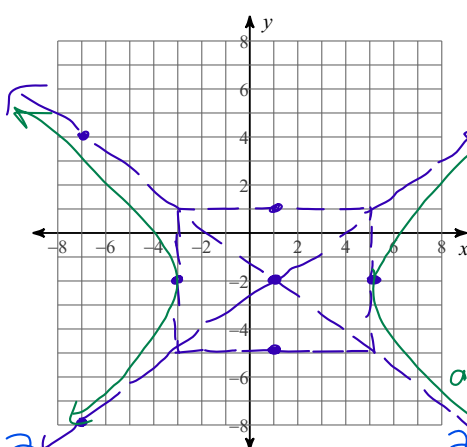
$y - 2 = \pm \frac{3}{4}(x - 1)$

- 1) vertices: (-1, -2) (-5, -2)
- 2)  $c^2 = a^2 + b^2 \rightarrow c^2 = 4 + 9 = 13 \rightarrow c = \sqrt{13}$   
 Foci:  $(-3 \pm \sqrt{13}, -2)$
- 3)  $y - y_1 = m(x - x_1) \rightarrow$  Point-slope Form  
 $y + 2 = \pm \frac{3}{2}(x + 3)$  (-3, -2)

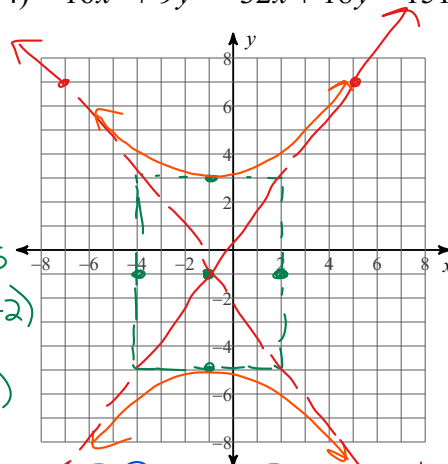
Both squarred and 1+ and 1-

3)  $9x^2 - 16y^2 - 18x - 64y - 199 = 0$

4)  $-16x^2 + 9y^2 - 32x + 18y - 151 = 0$



$c^2 = a^2 + b^2$   
 $= 16 + 9$   
 $c^2 = 25 \rightarrow c = 5$   
 Foci  $(-3, -2)$   $(5, -2)$   
 asymp  $y + 2 = \pm \frac{3}{4}(x - 1)$



$9x^2 - 18x + 9 - 16y^2 - 64y - 64 = 199 + 9 - 64$

$9(x^2 - 2x + 1) - 16(y^2 + 4y + 4)$

$\frac{9(x-1)^2}{144} - \frac{16(y+2)^2}{144} = \frac{144}{144}$

$\frac{(x-1)^2}{16} - \frac{(y+2)^2}{9} = 1$

4.)  $-16x^2 - 32x - 16 + 9y^2 + 18y + 9 = 151$

$-16(x^2 + 2x + 1) + 9(y^2 + 2y + 1) = 151 - 16 + 9$

$\frac{-16(x+1)^2}{144} + \frac{9(y+1)^2}{144} = \frac{144}{144}$

$\frac{-(x+1)^2}{9} + \frac{(y+1)^2}{16} = 1$

"center" (-1, -1)

$c^2 = 25$       asymp  $y + 1 = \pm \frac{4}{3}(x + 1)$

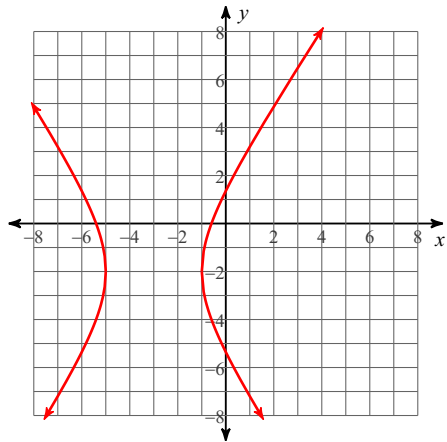
$c = 5$

Foci:  $(-1, 4)$   $(-1, -6)$

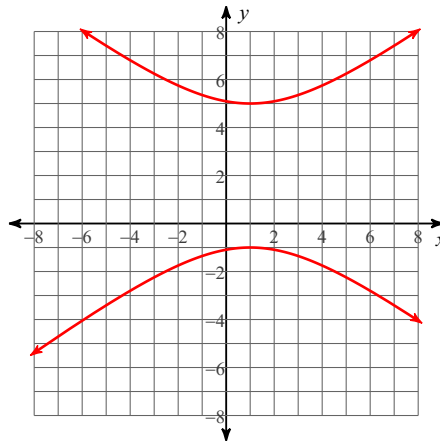
## Conic Sections Hyperbolas Notes

Identify the vertices, foci, and asymptotes of each. Then sketch the graph.

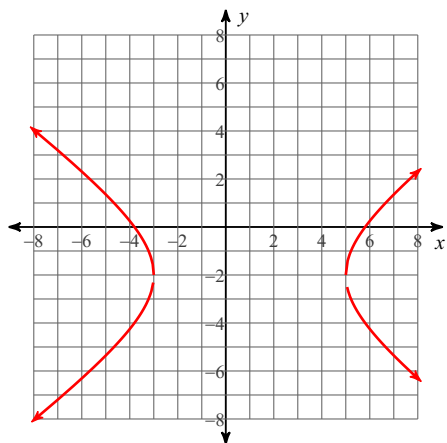
1) 
$$\frac{(x+3)^2}{4} - \frac{(y+2)^2}{9} = 1$$



2) 
$$\frac{(y-2)^2}{9} - \frac{(x-1)^2}{16} = 1$$



$$3) 9x^2 - 16y^2 - 18x - 64y - 199 = 0$$



$$4) -16x^2 + 9y^2 - 32x + 18y - 151 = 0$$

