

$$y - y_1 = m(x - x_1)$$

Pre Calculus

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Name _____

Conic Sections Hyperbolas Notes

Date _____ Period _____

Identify the vertices, foci, and asymptotes of each. Then sketch the graph.

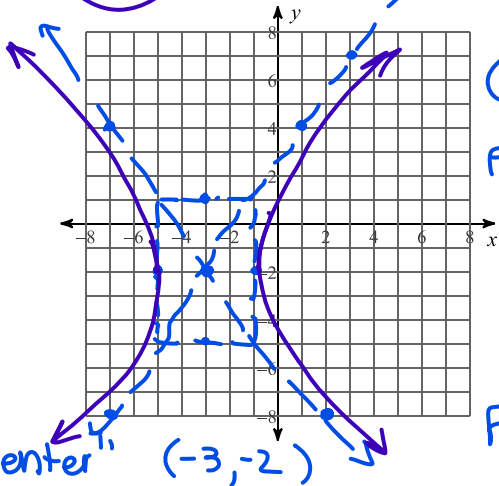
$$1) \frac{(x+3)^2}{4} - \frac{(y+2)^2}{9} = 1$$

Vertices
 $(-1, -2)$
 and
 $(-5, -2)$

Focal length
 $c^2 = a^2 + b^2$
 $c^2 = 4 + 9$
 $c^2 = 13$ $c = \sqrt{13}$

Foci: $(-3 \pm \sqrt{13}, -2)$

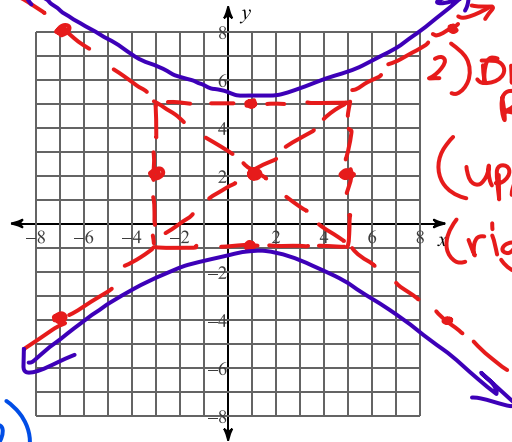
asymptotes $y + 2 = \pm \frac{3}{2}(x + 3)$



$$2) \frac{(y-2)^2}{9} - \frac{(x-1)^2}{16} = 1$$

1) "center" $(1, 2)$

2) Draw Rectangle
 (up/down 3)
 (right/left 4)



Vertices $(1, 5)$ $(1, -1)$

$c^2 = a^2 + b^2$

$c^2 = 9 + 16 = 25$

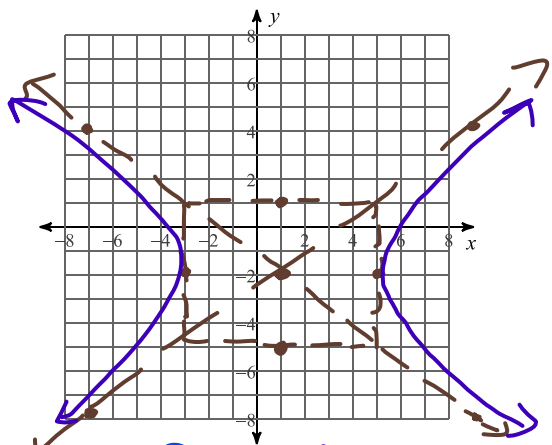
$c = 5$

Foci $(1, 2 \pm 5)$

$(1, 7), (1, -3)$

Asymptotes $y - 2 = \pm \frac{3}{4}(x - 1)$

$$3) 9x^2 - 16y^2 - 18x - 64y - 199 = 0$$



$$9x^2 - 18x + 9 - 16y^2 - 64y - 64 = 199 + 9 - 64$$

$$9(x^2 - 2x + 1) - 16(y^2 + 4y + 4)$$

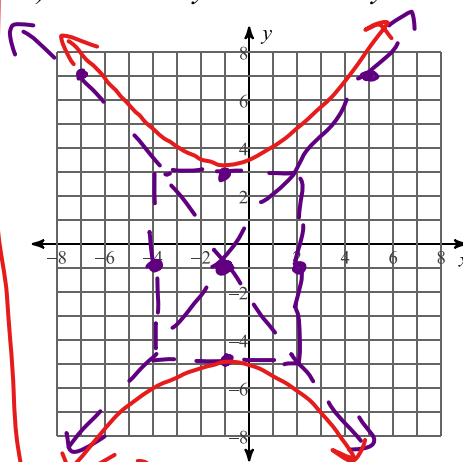
$$\frac{9(x-1)^2}{144} - \frac{16(y+2)^2}{144} = \frac{144}{144}$$

$$\boxed{\frac{(x-1)^2}{16} - \frac{(y+2)^2}{9} = 1}$$

Center (1, -2)

up/down 3 L/R 4

$$4) -16x^2 + 9y^2 - 32x + 18y - 151 = 0$$



c: (-1, 1)
up/down 4
L/R 3

$$-16x^2 - 32x - 16 + 9y^2 + 18y + 9 = 151 + 9 - 16$$

$$-16(x^2 + 2x + 1) + 9(y^2 + 2y + 1)$$

$$\frac{-16(x+1)^2}{144} + \frac{9(y+1)^2}{144} = \frac{144}{144}$$

$$\boxed{-\frac{(x+1)^2}{9} + \frac{(y+1)^2}{16} = 1}$$