

Converting Rectangular and Polar Form Notes

Convert each equation from rectangular to polar form.

→ turn into only r & / or θ

1) $y = -x\sqrt{3}$

get rid of x, y

$$\frac{y}{x} = -\sqrt{3}$$

$$\tan \theta = -\sqrt{3}$$

$$\theta = \frac{2\pi}{3}$$

2) $y = 5x$

$$\frac{y}{x} = 5$$

$$\tan \theta = 5$$

or

$$\theta = \tan^{-1}(5)$$

3) $(x+3)^2 + (y-1)^2 = 10$

$$x^2 + 6x + 9 + y^2 - 2y + 1 = 10$$

$$r^2 + 6r\cos\theta - 2r\sin\theta + 10 = 10$$

$$r^2 + 6r\cos\theta - 2r\sin\theta = 0$$

4) $(x+2)^2 + y^2 = 4$

$$x^2 + 4x + 4 + y^2 = 4$$

$$r^2 + 4r\cos\theta = 0$$

* -r → $r + 4\cos\theta = 0$

$$r = -4\cos\theta$$

5) $x = \frac{y^2}{4}$

$$r\cos\theta = \frac{r^2\sin^2\theta}{4}$$

$$\frac{4r\cos\theta}{r\cos\theta} = \frac{r^2\sin^2\theta}{r\cos\theta}$$

$$4 = r\tan\theta\sin\theta$$

$$r = 4\cot\theta\csc\theta$$

6) $y = \frac{x^2}{3}$

$$r\sin\theta = \frac{r^2\cos^2\theta}{3}$$

$$\frac{3r\sin\theta}{r\sin\theta} = \frac{r^2\cos^2\theta}{r\sin\theta} \rightarrow \frac{\cos\theta}{\sin\theta} \cos\theta$$

$$3 = r\cot\theta\cos\theta$$

$$r = 3\tan\theta\sec\theta$$

Convert each equation from polar to rectangular form.

7) $\theta = \frac{3\pi}{4}$

$\tan \theta = \tan \frac{3\pi}{4}$

$\frac{y}{x} = -1$

$y = -x$

8) $r = 4\cos \theta + 2\sin \theta$
 $r^2 = 4r\cos \theta + 2r\sin \theta$

$x^2 + y^2 = 4x + 2y$

$x^2 - 4x + y^2 - 2y = 0$

$(x-2)^2 + (y-1)^2 = 5$

9) $r = -6\cos \theta$

think about this graph
 off to left w/ $r = 3$
 c. $(-3, 0)$

$(x+3)^2 + y^2 = 9$

$r^2 = -6r\cos \theta$
 $x^2 + y^2 = -6x$
 $x^2 + 6x + y^2 = 0$

11) $r^2 = 4\csc(2\theta)$

$r^2 = \frac{4}{\sin(2\theta)}$

$r^2 \sin(2\theta) = 4$

$r^2 2\sin \theta \cos \theta = 4$

$2r\sin \theta r\cos \theta = 4$

$2yx = 4$

$xy = 2$

10) $r = 2\tan \theta \sec \theta$
 $\tan \theta = \frac{\sin \theta}{\cos \theta}$ $\sec \theta = \frac{1}{\cos \theta}$

$r = \frac{2\sin \theta}{\cos \theta} \cdot \frac{1}{\cos \theta}$

$r\cos \theta r\cos \theta = 2\sin \theta$

$x \cdot x = 2y$

$x^2 = 2y$

$r = 2\tan \theta \sec \theta$
 $r = \frac{2y}{x} \cdot \frac{1}{\cos \theta}$
 $r\cos \theta = \frac{2y}{x}$
 $x = \frac{2y}{x}$
 $x^2 = 2y$

12) $r^2 = 3\sec(2\theta)$

$r^2 = \frac{3}{\cos(2\theta)}$

$r^2 \cos(2\theta) = 3$

$r^2 (\cos^2 \theta - \sin^2 \theta) = 3$

$r^2 \cos^2 \theta - r^2 \sin^2 \theta = 3$

$x^2 - y^2 = 3$