

More Matrix Practice Notes

Solve each system.

1) $-x - 3y + 2z = -16$

$-2x - 3y + 4z = -20$

$-2x + 3y - 3z = 25$

$$\begin{array}{ccc|c} +1 & +3 & -2 & +16 \\ -2 & -3 & 4 & -20 \\ -2 & 3 & -3 & 25 \end{array}$$

$$\begin{array}{ccc|c} 1 & 3 & -2 & 16 \\ 2R_1 + R_2 & 0 & 3 & 0 & 12 \\ 2R_1 + R_3 & 0 & 9 & -7 & 57 \end{array}$$

$$\begin{array}{ccc|c} 1 & 3 & -2 & 16 \\ 0 & 3 & 0 & 12 \\ R_3 - 3R_2 & 0 & 0 & -7 & 21 \end{array}$$

$$\begin{array}{ccc|c} 1 & 3 & -2 & 16 \\ 0 & 3 & 0 & 12 \\ R_3 - 3R_2 & 0 & 0 & -7 & 21 \end{array}$$

$$\begin{array}{ccc|c} R_2/3 & 1 & 3 & -2 & 16 \\ 0 & 1 & 0 & 4 & 4 \end{array}$$

$$\begin{array}{ccc|c} R_3/-7 & 0 & 0 & 1 & -3 \end{array}$$

$$\begin{array}{ccc|c} R_1 - 3R_2 + 2R_3 & 1 & 0 & 0 & -2 \\ 0 & 1 & 0 & 4 & 4 \\ 0 & 0 & 1 & -3 & -3 \end{array}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -2 \\ 4 \\ -3 \end{bmatrix}$$

$$2) -x + y - 4z = -17$$

$$y - z = -2$$

$$x - 2y + 5z = -20$$

$$\begin{array}{ccc|c} +1 & -1 & +4 & +17 \\ 0 & 1 & -1 & -2 \\ 1 & -2 & 5 & -20 \end{array}$$

$$\begin{array}{l} -R_1 + R_3 \\ \begin{array}{ccc|c} 1 & -1 & 4 & 17 \\ 0 & 1 & -1 & -2 \\ 0 & -1 & 1 & -37 \end{array} \end{array}$$

$$\begin{array}{l} R_2 + R_3 \\ \begin{array}{ccc|c} 1 & -1 & 4 & 17 \\ 0 & 1 & -1 & -2 \\ 0 & 0 & 0 & -39 \end{array} \end{array}$$

No solution

$$\begin{aligned}
 3) \quad & 4x + 2y - 2z = 14 \\
 & -3x - 2y + z = -6 \\
 & -5x - 2y + 3z = -22
 \end{aligned}$$

$$\begin{array}{ccc|c}
 4 & 2 & -2 & 14 \\
 -3 & -2 & 1 & -6 \\
 -5 & -2 & 3 & -22
 \end{array}$$

$$\begin{array}{ccc|c}
 R_2 + R_1 & 1 & 0 & -1 & 8 \\
 & -3 & -2 & 1 & -6 \\
 & -5 & -2 & 3 & -22
 \end{array}
 \qquad
 \begin{array}{ccc|c}
 & 1 & 0 & -1 & 8 \\
 3R_1 + R_2 & 0 & -2 & -2 & 18 \\
 5R_1 + R_3 & 0 & -2 & -2 & 18
 \end{array}$$

$$\begin{array}{ccc|c}
 & 1 & 0 & -1 & 8 \\
 & 0 & -2 & -2 & 18 \\
 R_3 - R_2 & 0 & 0 & 0 & 0
 \end{array}$$

Infinite solutions

Simplify. Write "undefined" for expressions that are undefined.

PEMDAS

$$4) \begin{bmatrix} 0 & 0 & -1 \\ 6 & 6 & -3 \end{bmatrix} + \begin{bmatrix} -1 & 5 \\ -6 & -5 \end{bmatrix} \cdot \begin{bmatrix} 4 & -1 & -4 \\ 5 & 3 & 1 \end{bmatrix}$$

$2 \times 2 \checkmark \underline{2 \times 3} \rightarrow (2 \times 3)$

$$\begin{bmatrix} -4+25 & 1+5 & 4+5 \\ -24-25 & 6-15 & 24-5 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & -1 \\ 6 & 6 & -3 \end{bmatrix} + \begin{bmatrix} 21 & 16 & 9 \\ -49 & -9 & 19 \end{bmatrix} = \begin{bmatrix} 21 & 16 & 8 \\ -43 & -3 & 16 \end{bmatrix}$$

Solve each equation or state if there is no unique solution.

$$5) \begin{bmatrix} 16 \\ -10 \end{bmatrix} = 2B + \begin{bmatrix} 0 \\ -2 \end{bmatrix} - \begin{bmatrix} 0 \\ -2 \end{bmatrix}$$

$$- \begin{bmatrix} 0 \\ -2 \end{bmatrix}$$

$$\frac{\begin{bmatrix} 16 \\ -8 \end{bmatrix}}{2} = 2B \quad \xrightarrow{2} \text{ scalar}$$

$$B = \begin{bmatrix} 8 \\ -4 \end{bmatrix}$$

$$6) \begin{bmatrix} 2 \\ 2 \end{bmatrix} = \begin{bmatrix} -6 \\ -1 \end{bmatrix} + \begin{bmatrix} 4 & -2 \\ -3 & 3 \end{bmatrix} C$$

$$- \begin{bmatrix} -6 \\ -1 \end{bmatrix} \left(- \begin{bmatrix} -6 \\ -1 \end{bmatrix} \right)$$

$$\begin{bmatrix} 8 \\ 3 \end{bmatrix} = \begin{bmatrix} 4 & -2 \\ -3 & 3 \end{bmatrix} C$$

↓ Find the inverse

$$i) \quad 4 \cdot 3 - (-2)(-3) = 12 - 6 = 6$$

$$ii) \quad \frac{1}{6} \begin{bmatrix} 3 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 8 \\ 3 \end{bmatrix} = C$$

$$\frac{1}{6} \begin{bmatrix} 24+6 \\ 24+12 \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 30 \\ 36 \end{bmatrix} = \begin{bmatrix} 5 \\ 6 \end{bmatrix}$$

$$7) \begin{bmatrix} 10 & -8 \\ -3 & -19 \end{bmatrix} = \begin{bmatrix} -3 & -1 \\ 21 & 7 \end{bmatrix} Z - \begin{bmatrix} -10 & 6 \\ 3 & 8 \end{bmatrix}$$

$\rightarrow A$

No unique solution

i) Add But

ii) Find inverse

$$iii) \det A = -21 - -21 = 0$$

Answers to More Matrix Practice Notes

1) $(-2, 4, -3)$

4) $\begin{bmatrix} 21 & 16 & 8 \\ -43 & -3 & 16 \end{bmatrix}$

2) No solution

5) $\begin{bmatrix} 8 \\ -4 \end{bmatrix}$

3) Infinitely many solutions

6) $\begin{bmatrix} 5 \\ 6 \end{bmatrix}$

7) No unique solution