

**BC Parametrics Test Review**

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1. For  $0 \leq t \leq 13$ , an object travels along an elliptical path given by the parametric equations  $x = 3 \cos t$  and  $y = 4 \sin t$ . At the point where  $t = 13$ , the object leaves the path and travels along the line tangent to the path at that point. What is the slope of the line on which the object travels?

(A)  $-\frac{4}{3}$

(B)  $-\frac{3}{4}$

(C)  $-\frac{4 \tan 13}{3}$

(D)  $-\frac{4}{3 \tan 13}$  ✓

(E)  $-\frac{3}{4 \tan 13}$

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2. A curve  $C$  is defined by the parametric equations  $x = t^2 - 4t + 1$  and  $y = t^3$ . Which of the following is an equation of the line tangent to the graph of  $C$  at the point  $(-3, 8)$ ?

(A)  $x = -3$  ✓

(B)  $x = 2$

(C)  $y = 8$

(D)  $y = -\frac{27}{10}(x + 3) + 8$

(E)  $y = 12(x + 3) + 8$

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3. A curve is described by the parametric equations  $x = t^2 + 2t$  and  $y = t^3 + t^2$ . An equation of the line tangent to the curve at the point determined by  $t = 1$  is



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(A)  $2x - 3y = 0$

(B)  $4x - 5y = 2$

(C)  $4x - y = 10$

(D)  $5x - 4y = 7$  ✓

(E)  $5x - y = 13$

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4. If  $x=t^2-1$  and  $y=2e^t$ , then  $\frac{dy}{dx} =$

(A)  $\frac{e^t}{t}$  ✓

(B)  $\frac{2e^t}{t}$

(C)  $\frac{e^{|t|}}{t^2}$

(D)  $\frac{4e^t}{2t-1}$

(E)  $e^t$

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5. A particle moves along the curve  $xy=10$ . If  $x=2$  and  $dy/dt=3$ , what is the value of  $dx/dt$ ?



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(A)  $-5/2$

(B)  $-6/5$  ✓

(C)  $0$

(D)  $4/5$

(E)  $6/5$

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6. Consider the curve in the  $xy$ -plane represented by  $x=e^t$  and  $y=te^{-t}$  for  $t \geq 0$ . The slope of the line tangent to the curve at the point where  $x=3$  is

(A) 20.086

(B) 0.342

(C) -0.005

(D) -0.011 ✓

(E) -0.033

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7. If  $x=e^{2t}$  and  $y=\sin(2t)$ , then  $\frac{dy}{dx} =$



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(A)  $4e^{2t} \cos(2t)$

(B)  $\frac{e^{2t}}{\cos(2t)}$

(C)  $\frac{\sin(2t)}{2e^{2t}}$

(D)  $\frac{\cos(2t)}{2e^{2t}}$

(E)  $\frac{\cos(2t)}{e^{2t}}$



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8. For what values of  $t$  does the curve given by the parametric equations  $x = t^3 - t^2 - 1$  and  $y = t^4 + 2t^2 - 8t$  have a vertical tangent?

(A) 0 only

(B) 1 only

(C) 0 and  $\frac{2}{3}$  only

(D) 0,  $\frac{2}{3}$ , and 1

(E) No value



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9. A curve in the plane is defined parametrically by the equations  $x = t^3 + t$  and  $y = t^4 + 2t^2$ . An equation of the line tangent to the curve at  $t=1$  is



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(A)  $y=2x$

(B)  $y=8x$

(C)  $y=2x-1$  ✓

(D)  $y=4x-5$

(E)  $y=8x+13$

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10. If  $x = t^2 + 1$  and  $y = t^3$ , then  $d^2y/dx^2 =$

(A)  $3/4t$  ✓

(B)  $3/2t$

(C)  $3t$

(D)  $6t$

(E)  $3/2$

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11. The length of a curve from  $x = 1$  to  $x = 4$  is given by  $\int_1^4 \sqrt{1 + 9x^4} dx$ . If the curve contains the point  $(1, 6)$ , which of the following could be an equation for this curve?



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(A)  $y = 3 + 3x^2$

(B)  $y = 5 + x^3$  ✓

(C)  $y = 6 + x^3$

(D)  $y = 6 - x^3$

(E)  $y = \frac{16}{5} + x + \frac{9}{5}x^5$

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12. Which of the following integrals gives the length of the graph  $y = \sin(\sqrt{x})$  between  $x = a$  and  $x = b$ , where  $0 < a < b$ ?

(A)  $\int_a^b \sqrt{x + \cos^2(\sqrt{x})} dx$

(B)  $\int_a^b \sqrt{1 + \cos^2(\sqrt{x})} dx$

(C)  $\int_a^b \sqrt{\sin^2(\sqrt{x}) + \frac{1}{4x} \cos^2(\sqrt{x})} dx$

(D)  $\int_a^b \sqrt{1 + \frac{1}{4x} \cos^2(\sqrt{x})} dx$  ✓

(E)  $\int_a^b \sqrt{\frac{1 + \cos^2(\sqrt{x})}{4x}} dx$

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13. The length of the curve  $y = \ln \sec x$  from  $x=0$  to  $x=b$ , where  $0 < b < \frac{\pi}{2}$ , may be expressed by which of the following integrals?



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(A)  $\int_0^b \sec x dx$



(B)  $\int_0^b \sec^2 x dx$

(C)  $\int_0^b (\sec x \tan x) dx$

(D)  $\int_0^b \sqrt{1 + (\ln \sec x)^2} dx$

(E)  $\int_0^b \sqrt{1 + (\sec^2 x \tan^2 x)} dx$

14. Which of the following gives the length of the path described by the parametric equations  $x = \sin(t^3)$  and  $y = e^{5t}$  from  $t=0$  to  $t=\pi$ ?

(A)  $\int_0^\pi \sqrt{\sin^2(t^3) + e^{10t}} dt$

(B)  $\int_0^\pi \sqrt{\cos^2(t^3) + e^{10t}} dt$

(C)  $\int_0^\pi \sqrt{9t^4 \cos^2(t^3) + 25e^{10t}} dt$



(D)  $\int_0^\pi \sqrt{3t^2 \cos(t^3) + 5e^{5t}} dt$

(E)  $\int_0^\pi \sqrt{\cos^2(3t^2) + e^{10t}} dt$

15. The length of the curve determined by the equations  $x = t^2$  and  $y=t$  from  $t=0$  to  $t=4$  is



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(A)  $\int_0^4 \sqrt{4t+1} dt$

(B)  $2 \int_0^4 \sqrt{t^2+1} dt$

(C)  $\int_0^4 \sqrt{2t^2+1} dt$

(D)  $\int_0^4 \sqrt{4t^2+1} dt$



(E)  $2\pi \int_0^4 \sqrt{4t^2+1} dt$

16. The length of the path described by the parametric equations  $x = \cos^3 t$  and  $y = \sin^3 t$ , for  $0 \leq t \leq \frac{\pi}{2}$  is given by

(A)  $\int_0^{\frac{\pi}{2}} \sqrt{3\cos^2 t + 3\sin^2 t} dt$

(B)  $\int_0^{\frac{\pi}{2}} \sqrt{-3\cos^2 t \sin t + 3\sin^2 t \cos t} dt$

(C)  $\int_0^{\frac{\pi}{2}} \sqrt{9\cos^4 t + 9\sin^4 t} dt$

(D)  $\int_0^{\frac{\pi}{2}} \sqrt{9\cos^4 t \sin^2 t + 9\sin^4 t \cos^2 t} dt$



(E)  $\int_0^{\frac{\pi}{2}} \sqrt{\cos^6 t + \sin^6 t} dt$

17. At time  $t \geq 0$ , a particle moving in the  $xy$ -plane has velocity vector given by  $v(t) = \langle t^2, 5t \rangle$ . What is the acceleration vector of the particle at time  $t=3$ ?





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(A)  $\left\langle 9, \frac{45}{2} \right\rangle$

(B)  $\langle 6, 5 \rangle$



(C)  $\langle 2, 0 \rangle$

(D)  $\sqrt{306}$

(E)  $\sqrt{61}$

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18. In the  $xy$ -plane, a particle moves along the parabola  $y = x^2 - x$  with a constant speed of  $2\sqrt{10}$  units per second. If  $\frac{dx}{dt} > 0$ , what is the value of  $\frac{dy}{dt}$  when the particle is at the point  $(2, 2)$  ?

(A)  $\frac{2}{3}$

(B)  $\frac{2\sqrt{10}}{3}$

(C) 3

(D) 6



(E)  $6\sqrt{10}$

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19. A particle moves on the curve  $y = \ln x$  so that the  $x$ -component has velocity  $x'(t) = t + 1$  for  $t \geq 0$ . At time  $t=0$ , the particle is at the point  $(1, 0)$ . At time  $t=1$ , the particle is at the point



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(A)  $(2, \ln 2)$

(B)  $(e^2, 2)$

(C)  $(\frac{5}{2}, \ln \frac{5}{2})$



(D)  $(3, \ln 3)$

(E)  $(\frac{3}{2}, \ln \frac{3}{2})$

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20. A particle moves in the  $xy$ -plane so that at any time  $t$  its coordinates are  $x = t^2 - 1$  and  $y = t^4 - 2t^3$ . At  $t = 1$ , its acceleration vector is

(A)  $(0, -1)$

(B)  $(0, 12)$

(C)  $(2, -2)$

(D)  $(2, 0)$



(E)  $(2, 8)$

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21. If a particle moves in the  $xy$ -plane so that at time  $t > 0$  its position vector is  $(\ln(t^2 + 2t), 2t^2)$ , then at time  $t = 2$ , its velocity vector is



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**A**  $(\frac{3}{4}, 8)$



**B**  $(\frac{3}{4}, 4)$

**C**  $(\frac{1}{8}, 8)$

**D**  $(\frac{1}{8}, 4)$

**E**  $(-\frac{5}{16}, 4)$

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22. A particle moves on a plane curve so that at any time  $t > 0$  its  $x$ -coordinate is  $t^3 - t$  and its  $y$ -coordinate is  $(2t - 1)^3$ . The acceleration vector of the particle at  $t = 1$  is

**A**  $(0, 1)$

**B**  $(2, 3)$

**C**  $(2, 6)$

**D**  $(6, 12)$

**E**  $(6, 24)$



23. For any time  $t \geq 0$ , if the position of a particle in the  $xy$ -plane is given by  $x = t^2 + 1$  and  $y = \ln(2t + 3)$ , then the acceleration vector is



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(A)  $(2t, 2/(2t+3))$

(B)  $(2, -4/(2t+3)^2)$

(C)  $(2, 4/(2t+3)^2)$

(D)  $(2, 2/(2t+3)^2)$

(E)  $(2t, -4/(2t+3)^2)$

