Rationales for Multiple Choice Questions:

| Q1 |  |
| :---: | :---: |
| $A$ | The student found ${ }^{\prime}(3)$ |
| $B$ | This answer is correct |
| $C$ | The student found $x(3)$ |
| $D$ | The student found $v(3)$ |


| Q2 |  |
| :---: | :---: |
| $A$ | The student found time when $a(t)=0$ |
| $B$ | The student found the time when $v(t)=0$ |
| $C$ | The student found $a(t)$ when $v(t)=0$ |
| $D$ | This answer is correct |


| Q3 |  |
| :---: | :---: |
| $A$ | The student averaged the avg. velocity of each subinterval |
| $B$ | The student added up the given $v(t)$ values and divided by10 |
| $C$ | This answer is correct |
| $D$ | The student chose the middle velocity value in the table |


| Q4 |  |
| :---: | :---: |
| $A$ | The student averaged the $v(1)$ and $v(4)$ |
| $B$ | The student found the approx. $a(t)$ on $[0,4]$ |
| $C$ | The student found the approx. $a(t)$ on $[0,10]$ |
| $D$ | This answer is correct |


| Q5 |  |
| :---: | :---: |
| $A$ | This answer is correct |
| $B$ | The student found a Left Riemann sum |
| $C$ | The student found a trapezoidal sum |
| $D$ | The student shows a misunderstanding of a Riemann sum |


| $A$ | The student included a negative when differentiating $\sin (t)$ |
| :---: | :---: |
| $B$ | The student failed to use the chain rule |
| $C$ | This answer is correct |
| $D$ | The student incorrectly evaluated the trig function |


| Q7 |  |
| :---: | :---: |
| $A$ | The student found the final position with a $R R S$ |
| $B$ | This answer is correct |
| $C$ | The student used a Left Riemann Sum |
| $D$ | The student multiplied each $t$ value with the corresponding $v(t)$ and added |

Q8

| $A$ | The student only found the decrease in velocity from 1 to 3 sec |
| :---: | :---: |
| $B$ | This answer is correct |
| $C$ | The student found the average acceleration over the entire interval |
| $D$ | The student approximated $v(2)$ |


|  |  |
| :---: | :---: |
| A | The student found the displacement of the bug after 8 seconds |
| $B$ | This answer is correct |
| $C$ | The student found the total distance the bug traveled over the 8 seconds |
| $D$ | The student added the initial condition to the total distance |


| Q10 |  |
| :---: | :---: |
| A | The student found the displacement of the bug after 8 seconds |
| B | The student found the position of the bug after 8 seconds |
| C | This answer is correct |
| $D$ | The student added the initial condition to the total distance |

Q11

| $A$ | This answer is correct |
| :---: | :---: |
| $B$ | The student found when the bug's position is negative |
| $C$ | The student found when the bug was moving to the right |
| $D$ | The student found when $a(t)>0$ |


| Q12 |  |
| :---: | :---: |
| $A$ | The student found $v(10)$ and divided by 10 |
| $B$ | The student found the average acceleration over the interval |
| $C$ | This answer is correct |
| $D$ | The student found the average position of the bug |


| 13 |  |
| :---: | :---: |
| $A$ | The student found $v(7)$ |
| $B$ | The student assigned a negative value to $a(7)$ |
| $C$ | This answer is correct |
| $D$ | The student found the speed of the toy at $t=7$ |


| Q14 |
| :--- |
| $A$ The student found when $v^{\prime}(t)=0$ <br> $B$ This answer is correct <br> $C$ The student found when $v^{\prime}(t)$ is undefined <br> $D$ The student found the critical values for $v(t)$ |


| Q15 |  |
| :---: | :---: |
| $A$ | The student only found when $v(t)>0$ and $v^{\prime}(t)>0$ |
| $B$ | This answer is correct |
| $C$ | The student found when the car has a positive acceleration |
| $D$ | The student found when the car is speeding up |


| Q16 |  |
| :---: | :---: |
| $A$ | The student chose the initial time instead of finding $v(t)=0$ |
| $B$ | This answer is correct |
| $C$ | The student incorrectly factored $y(t)$ and solved fort $t$ |
| $D$ | The student found when $y(t)=0$ |


| Q17 |  |
| :---: | :---: |
| $A$ | The student found when the ball was slowing down |
| $B$ | The student found when $v(t)<0$ |
| $C$ | The student incorrectly handled the coefficient 5 in the problem |
| $D$ | This answer is correct |

Q18

| $A$ | The student used $t=0$ as a critical value when solving $e^{t}=0$ |
| :---: | :---: |
| $B$ | The student $a(t)$ incorrectly |
| $C$ | The student did not use product rule when finding a $(t)$ |
| $D$ | This answer is correct |

Q19

| $A$ | This answer is correct |
| :---: | :---: |
| $B$ | The student did not include a negative when differentiating $\cos (t)$ |
| $C$ | The student did not use the chain rule when differentiating |
| $D$ | The student did not use the chain rule when differentiating |

Q20

| $A$ | This answer is correct |
| :---: | :---: |
| $B$ | The student incorrectly differentiated $\cos (t)$ and did not include a negative |
| $C$ | The student incorrectly found the critical values after differentiating |
| $D$ | The student found when the ball is moving left |

Q21

| $A$ | The student incorrectly integrated $\sin (t)$ as $\cos (t)$ instead of $-\cos (t)$ |
| :---: | :---: |
| $B$ | This answer is correct |
| $C$ | The student failed to integrate velocity |
| $D$ | The student did not divide by $\pi$ to find the average velocity |


| Q22 |  |
| :---: | :---: |
| $A$ | The student found only one of the correct intervals |
| $B$ | The student found only when $v(t)<0$ |
| $C$ | This answer is correct |
| $D$ | The student misinterpreted the sign charts for $v(t)$ and $a(t)$ |

Q23

| $A$ | The student averaged $v(0)$ and $v(2)$ |
| :---: | :---: |
| $B$ | This answer is correct |
| $C$ | The student found $v(4)$ |
| $D$ | The student found the average acceleration of the bug |


| Q24 |  |
| :---: | :---: |
| $A$ | The student did not include the initial position |
| $B$ | This answer is correct |
| $C$ | The student found the total distance traveled |
| $D$ | The student used the total distance traveled with the initial condition |

Q25

| $A$ | The student did not consider when $v^{\prime}(t)$ is undefined when checking intervals |
| :---: | :---: |
| $B$ | The student did not consider when $v^{\prime}(t)$ is undefined when checking intervals |
| $C$ | The student incorrectly checked values in the interval |
| $D$ | This answer is correct |


| Q26 |  |
| :---: | :---: |
| A | The student did not include the initial position |
| $B$ | This answer is correct |
| $C$ | The student did not include the initial position and found total distance |
| $D$ | The student found total distance plus initial position |

Q27

| $A$ | The student found the net displacement |
| :---: | :---: |
| $B$ | The student found the final position |
| $C$ | This answer is correct |
| $D$ | The student incorrectly used the initial position |


| Q28 |  |
| :---: | :---: |
| $A$ | The student found the time when $a(t)=5$ |
| $B$ | This answer is correct |
| $C$ | The student found $a(5)$ |
| $D$ | The student found $v(5)$ |


| Q29 |  |
| :---: | :---: |
| $A$ | The student found displacement |
| $B$ | The student found the final position |
| $C$ | This answer is correct |
| $D$ | The student added 5 to the total distance |


| Q30 |
| :---: | :---: |
| $A$ The student did not know how to apply the IVT <br> $B$ The student did not know how to correctly apply IVT multiple times <br> $C$ The student only identified two of the three times guaranteed by IVT <br> $D$ This answer is correct |

Q31

| $A$ | The student found $v(6)-v(0)$ |
| :---: | :---: |
| $B$ | The student found $v(6)$ |
| $C$ | The student found the net displacement of the particle |
| $D$ | This answer is correct |


| Q32 |  |
| :---: | :---: |
| $A$ | The student found when $v(t)>0$ |
| $B$ | This answer is correct |
| $C$ | The student found when $v(t)<0$ and $a(t)=0$ |
| $D$ | The student found when $a(t)>0$ but $v(t)<0$ |

Q33

| $A$ | The student only checked the endpoints |
| :---: | :---: |
| $B$ | This answer is correct |
| $C$ | The student found when $a(t)=0$ |
| $D$ | The student found when $a(t)$ is a maximum |


| Q34 |  |
| :---: | :---: |
| $A$ | The student found the net displacement |
| $B$ | This answer is correct |
| $C$ | The student added the initial position to the distance |
| $D$ | The student found the final position |


| Q35 |  |
| :---: | :---: |
| $A$ | The student found the net displacement of the particle over the interval |
| $B$ | The student found net displacement and did not use u-sub properly when integrating |
| $C$ | This answer is correct |
| $D$ | The student did not use u-sub properly when integrating |


| Q36 |  |
| :---: | :---: |
| $A$ | The student did not divide by 5 to find the average value |
| $B$ | This answer is correct |
| $C$ | The student added up each $v(t)$ in the table and divided by 5 |
| $D$ | The student found the average acceleration |

Q37

| A | This answer is correct |
| :---: | :---: |
| $B$ | The student added the position at 5 instead of subtracting |
| $C$ | The student found a Right Riemann sun but did not use the initial position value |
| $D$ | The student found total distance traveled with the initial condition |

Q38

| $A$ | The student found when $v(t)>0$ |
| :---: | :---: |
| $B$ | This answer is correct |
| $C$ | The student found when $a(t)>0$ |
| $D$ | The student found when the bug is slowing down |


| Q39 |  |
| :---: | :---: |
| $A$ | This answer is correct |
| $B$ | The student found $v(1)$ |
| $C$ | The student found the displacement |
| $D$ | The student found the total distance traveled |

Q40

| $A$ | The student found the displacement |
| :---: | :---: |
| $B$ | The student found the position at $t=4$ |
| $C$ | The student found the displacement and took the absolute value |
| $D$ | This answer is correct |


| Q41 |
| :--- |
| $A$ The student found when $t=0$ <br> $B$ The student found the $a(t)$ was a minimum <br> $C$ The student found when $a(t)=0$ <br> $D$ This answer is correct |


| Q42 |  |
| :---: | :---: |
| $A$ | The student took the absolute value of displacement |
| $B$ | This answer is correct |
| $C$ | The student found $v(1)-v(0)$ |
| $D$ | The student found $v^{\prime}(1)$ |


| Q43 |  |
| :---: | :---: |
| $A$ | The student found $a(0)$ |
| $B$ | This answer is correct |
| $C$ | The student found $v(0)$ |
| $D$ | The student only found the time when $v(t)=0$ |


| Q44 |  |
| :---: | :---: |
| $A$ | The student found the absolute value of $v(0)$ |
| $B$ | The student found $a(t)$ when the bug is at rest |
| $C$ | This answer is correct |
| $D$ | The student found when $a(t)=0$ |


| Q45 |  |
| :---: | :---: |
| $A$ | The student assumed $a(t)=0$ when $v(t)=0$ |
| $B$ | The student found $a(0)$ |
| $C$ | This answer is correct |
| $D$ | The student found the time when the particle is at rest |


| Q46 |
| :--- |
| $A$ This answer is correct <br> $B$ The student did not consider $v(3)$ <br> $C$ The student confused $v(t)$ and $a(3)$ <br> $D$ The student confused $a(t)$ and $v(t)$ |


| Q47 |  |
| :---: | :---: |
| A | The student found the particles are both moving toward the right |
| $B$ | The student found when one particle was moving right but the second was at rest |
| $C$ | This answer is correct |
| $D$ | The student found when the particles were moving in opposite directions |


| Q48 |  |
| :---: | :---: |
| $A$ | The student found when the particles must move toward each other |
| $B$ | This answer is correct |
| $C$ | The student incorrectly included the first interval |
| $D$ | The student found two intervals that would not be guaranteed to cross paths |


| Q49 |  |
| :---: | :---: |
| A | The student found the average velocity of each interval and averaged the answers |
| $B$ | The student found the average value of just the endpoints |
| C | This answer is correct |
| $D$ | The student found the average values of the intervals separately and added |


| Q50 |  |
| :---: | :---: |
| $A$ | The student found when both particles had positive acceleration |
| $B$ | The student found when particle $B$ had great velocity than particle $A$ |
| $C$ | This answer is correct |
| $D$ | The student found when the velocities have opposite signs |


| Q51 |  |
| :---: | :---: |
| $A$ | This answer is correct |
| $B$ | The student found the difference in total distance traveled |
| $C$ | The student did not include the initial position |
| $D$ | The student included initial position but used total distance |


| Q52 |  |
| :---: | :---: |
| A | The student found when the particles' position had opposite signs |
| B | The student found when the particles' velocity had opposite signs |
| C | The student did not include the full interval |
| $D$ | This answer is correct |


| Q53 |  |
| :---: | :---: |
| $A$ | The student the position of particle $A$ when Particle B started to move left |
| $B$ | This answer is correct |
| $C$ | The student found the time when the particles crossed paths |
| $D$ | The student found the total distance traveled by particle $B$ |


| Q54 |  |
| :---: | :---: |
| $A$ | The student found when $v(t)>0$ |
| $B$ | This answer is correct |
| $C$ | The student found when $a(t)$ is increasing |
| $D$ | The student found when $a(t)>0$ |

