

## Integrals Practice (All types including U-sub, etc.)

Name \_\_\_\_\_

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1.  $\int_0^{\frac{\pi}{2}} \frac{\cos \theta}{\sqrt{1 + \sin \theta}} d\theta =$

(A)  $-2(\sqrt{2} - 1)$

(B)  $-2\sqrt{2}$

(C)  $2\sqrt{2}$

(D)  $2(\sqrt{2} - 1)$

(E)  $2(\sqrt{2} + 1)$

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2.  $\int_0^1 (3x - 2)^2 dx =$

(A)  $-\frac{7}{3}$

(B)  $-\frac{7}{9}$

(C)  $\frac{1}{9}$

(D) 1

(E) 3

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3.  $\int \frac{x dx}{\sqrt{3x^2 + 5}} =$



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(A)  $\frac{1}{9}(3x^2 + 5)^{\frac{3}{2}} + c$

(B)  $\frac{1}{4}(3x^2 + 5)^{\frac{3}{2}} + c$

(C)  $\frac{1}{12}(3x^2 + 5)^{\frac{1}{2}} + c$

(D)  $\frac{1}{3}(3x^2 + 5)^{\frac{1}{2}} + c$

(E)  $\frac{3}{2}(3x^2 + 5)^{\frac{1}{2}} + c$

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4.  $\int \cos(3x) dx =$

(A)  $-3 \sin(3x) + c$

(B)  $-\frac{1}{3} \sin(3x) + c$

(C)  $\frac{1}{3} \sin(3x) + c$

(D)  $\sin(3x) + c$

(E)  $3 \sin(3x) + c$

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5.  $\int \frac{x}{x^2 - 4} dx =$



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- (A)  $\frac{-1}{4(x^2-4)^2} + C$
- (B)  $\frac{1}{2(x^2-4)} + C$
- (C)  $\frac{1}{2} \ln|x^2 - 4| + C$
- (D)  $2 \ln|x^2 - 4| + C$
- (E)  $\frac{1}{2} \arctan\left(\frac{x}{2}\right) + C$
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6. Using the substitution  $u = \sin(2x)$ ,  $\int_{\pi/6}^{\pi/2} \sin^5(2x) \cos(2x) dx$  is equivalent to

- (A)  $-2 \int_{1/2}^1 u^5 du$
- (B)  $\frac{1}{2} \int_{1/2}^1 u^5 du$
- (C)  $\frac{1}{2} \int_0^{\sqrt{3}/2} u^5 du$
- (D)  $\frac{1}{2} \int_{\sqrt{3}/2}^0 u^5 du$
- (E)  $2 \int_{\sqrt{3}/2}^0 u^5 du$
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7.  $\int (3x + 1)^5 dx =$



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- (A)  $\frac{(3x+1)^6}{18} + C$
- (B)  $\frac{(3x+1)^6}{6} + C$
- (C)  $\frac{(3x+1)^6}{2} + C$
- (D)  $\frac{\left(\frac{3x^2}{2} + x\right)^6}{2} + C$
- (E)  $\left(\frac{3x^2}{2} + x\right)^5 + C$
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8.  $\int_0^1 x\sqrt{1+8x^2} dx =$

- (A)  $\frac{1}{24}$
- (B)  $\frac{13}{12}$
- (C)  $\frac{9}{8}$
- (D)  $\frac{52}{3}$
- (E) 18
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9. Let  $f$  be a function such that  $\int_6^{12} f(2x) dx = 10$ . Which of the following must be true?



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(A)  $\int_{12}^{24} f(t) dt = 5$

(B)  $\int_{12}^{24} f(t) dt = 20$

(C)  $\int_6^{12} f(t) dt = 5$

(D)  $\int_6^{12} f(t) dt = 20$

(E)  $\int_3^6 f(t) dt = 5$

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10.  $\int_2^4 \frac{dx}{5-3x} =$

(A)  $-\ln 7$

(B)  $-\frac{\ln 7}{3}$

(C)  $\frac{\ln 7}{3}$

(D)  $\ln 7$

(E)  $3 \ln 7$

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11. The function  $f$  is continuous and  $\int_0^8 f(u) du = 6$ . What is the value of  $\int_1^3 xf(x^2 - 1) dx$ ?



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(A)  $\frac{3}{2}$

(B) 3

(C) 6

(D) 12

(E) 24

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12.  $\int_0^1 e^{-4x} dx =$

(A)  $\frac{-e^{-4}}{4}$

(B)  $-4e^{-4}$

(C)  $e^{-4} - 1$

(D)  $\frac{1}{4} - \frac{e^{-4}}{4}$

(E)  $4 - 4e^{-4}$ 

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13. Using the substitution  $u = 2x + 1$ ,  $\int_0^2 \sqrt{2x + 1} dx$  is equivalent to



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(A)  $\frac{1}{2} \int_{-1/2}^{1/2} \sqrt{u} \, du$

(B)  $\frac{1}{2} \int_0^2 \sqrt{u} \, du$

(C)  $\frac{1}{2} \int_1^5 \sqrt{u} \, du$

(D)  $\int_0^2 \sqrt{u} \, du$

(E)  $\int_1^5 \sqrt{u} \, du$

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14. If  $\int_0^k \frac{x}{x^2 + 4} \, dx = \frac{1}{2} \ln 4$ , where  $k > 0$ , then  $k =$

(A) 0

(B)  $\sqrt{2}$

(C) 2

(D)  $\sqrt{12}$

(E)  $\frac{1}{2} \tan(\ln \sqrt{2})$

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15.  $\int \frac{e^{\sqrt{x}}}{\sqrt{x}} \, dx =$



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- (A)  $2e^{\sqrt{x}} + c$
- (B)  $\frac{1}{2}e^{\sqrt{x}} + c$
- (C)  $e^{\sqrt{x}} + c$
- (D)  $2\sqrt{x}e^{\sqrt{x}} + c$
- (E)  $\frac{1}{2}\frac{e^{\sqrt{x}}}{\sqrt{x}} + c$
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16. If the substitution  $\sqrt{x} = \sin y$  is made in the integrand of  $\int_0^{1/2} \frac{\sqrt{x}}{\sqrt{1-x}} dx$ , the resulting integral is

- (A)  $\int_0^{1/2} \sin^2 y dy$
- (B)  $2 \int_0^{1/2} \frac{\sin^2 y}{\cos y} dy$
- (C)  $2 \int_0^{\pi/4} \sin^2 y dy$
- (D)  $\int_0^{\pi/4} \sin^2 y dy$
- (E)  $2 \int_0^{\pi/6} \sin^2 y dy$
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17.  $\int_0^5 \sqrt{\frac{5-x}{5}} dx =$





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(A)  $\frac{2}{3}$

(B)  $\frac{10}{3}$

(C) 5

(D)  $\frac{50\sqrt{5}}{3}$

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18.  $\int_0^{\ln 2} \frac{e^x}{1 + (e^x - 1)^2} dx =$

(A)  $\arctan(\ln 2)$

(B)  $\ln 2$

(C)  $\pi/4$

(D)  $\pi/2$

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19. Using the substitution  $u = x + 1$   $\int \frac{x}{\sqrt{x+1}} dx$  is equivalent to

(A)  $\int \frac{1}{u+1} du$

(B)  $\int u^{-1/2} du$

(C)  $\int (u^{1/2} - u^{-1/2}) du$

(D)  $(u - 1) \int u^{-1/2} du$

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20. 
$$\int_1^e \frac{x^2 + 1}{x} dx =$$

(A)  $\frac{e^2 - 1}{2}$

(B)  $\frac{e^2 + 1}{2}$

(C)  $\frac{e^2 + 2}{2}$

(D)  $\frac{e^2 - 1}{e^2}$

(E)  $\frac{2e^2 - 8e + 6}{3e}$ 

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21. An antiderivative for  $\frac{1}{x^2 - 2x + 2}$  is

(A)  $-(x^2 - 2x + 2)^{-2}$

(B)  $\ln(x^2 - 2x + 2)$

(C)  $\ln\left|\frac{x-2}{x+1}\right|$

(D)  $\operatorname{arcsec}(x-1)$

(E)  $\arctan(x-1)$ 

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22. 
$$\int_1^2 \frac{x^2 - x - 5}{x + 2} dx =$$



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(A)  $-\frac{3}{2} + \ln \frac{4}{3}$

(B)  $-\frac{25}{21}$

(C)  $\frac{5}{2} + 3 \ln \frac{3}{4}$

(D)  $\frac{23}{45}$

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23.  $\int \frac{6x^2 - 4x - 25}{x - 2} dx =$

(A)  $3x^2 + 8x - 9 \ln |x - 2| + C$

(B)  $3x^2 + 8x + \frac{9}{(x-2)^2} + C$

(C)  $(2x^3 - 2x^2 - 25x) \ln |x - 2| + C$

(D)  $\frac{2x^3 - 2x^2 - 25x}{\frac{x^2}{2} - 2x} + C$

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24. If  $\int_1^2 f(x - c) dx = 5$  where  $c$  is a constant, then  $\int_{1-c}^{2-c} f(x) dx =$



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(A)  $5+c$

(B)  $5$

(C)  $5-c$

(D)  $c-5$

(E)  $-5$

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25. Which of the following are equivalent to  $\int_2^4 \frac{2x+5}{5-x} dx$ ?

1.  $\frac{\int_2^4 (2x+5) dx}{\int_2^4 (5-x) dx}$

2.  $\int_2^4 \left( -2 + \frac{15}{5-x} \right) dx$

3.  $\int_1^3 \left( \frac{15}{u} - 2 \right) du$

(A) I only

(B) II only

(C) III only

(D) II and III only

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26.  $\int \frac{8}{\sqrt{12-x^2-4x}} dx =$



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(A)  $16\sqrt{12 - x^2 - 4x} + C$

(B)  $2 \sin^{-1}\left(\frac{x+2}{4}\right) + C$

(C)  $8 \sin^{-1}\left(\frac{x-2}{4}\right) + C$

(D)  $8 \sin^{-1}\left(\frac{x+2}{4}\right) + C$

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27.  $\int \frac{4x^3}{2x+3} dx =$

(A)  $\frac{x^4}{x^2+3x} + C$

(B)  $x^4 \ln|2x+3| + C$

(C)  $\frac{2}{3}x^3 - \frac{3}{2}x^2 + \frac{9}{2}x - \frac{27}{4}\ln|2x+3| + C$

(D)  $\frac{2}{3}x^3 - \frac{3}{2}x^2 + \frac{9}{2}x - \frac{27}{2}\ln|2x+3| + C$

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28.  $\int \frac{4x^4 + 3}{4x^5 + 15x + 2} dx =$

(A)  $-\frac{1}{5(4x^5+15x+2)^2} + C$

(B)  $\frac{\frac{4}{5}x^5+3x}{\frac{2}{3}x^6+\frac{15}{2}x^2+2x} + C$

(C)  $\frac{1}{5}\ln|4x^5 + 15x + 2| + C$

(D)  $5 \ln|4x^5 + 15x + 2| + C$

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29. 
$$\int_0^1 (x^3 + x)(x^4 + 2x^2 + 9)^{\frac{1}{2}} dx =$$

Ⓐ  $\frac{1}{6}$

Ⓑ  $\frac{2}{3}$

Ⓒ  $4\sqrt{3} - \frac{9}{2}$

Ⓓ  $16\sqrt{3} - 18$ 

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30. 
$$\int \frac{1}{\sqrt{9-x^2}} dx =$$

Ⓐ  $\ln(\sqrt{9-x^2}) + C$

Ⓑ  $\frac{1}{3}\sin^{-1}\left(\frac{x}{3}\right) + C$

Ⓒ  $3\sin^{-1}\left(\frac{x}{3}\right) + C$

Ⓓ  $\sin^{-1}\left(\frac{x}{3}\right) + C$ 

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